### Geol 600 Notable Historical Earthquakes

Source mechanisms and body wave radiation patterns

#### Force Couples:

Forces must occur in opposing directions to conserve momentum



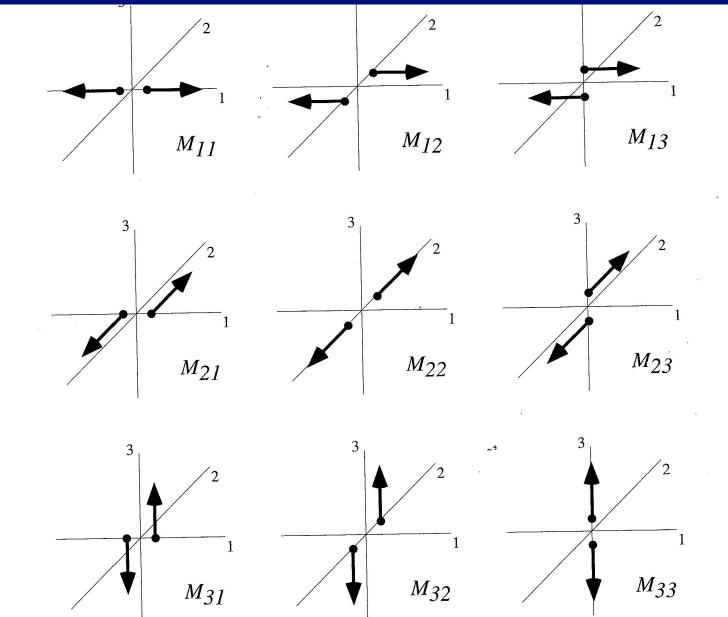
9 Force Couples  $M_{ij}$  (the moment tensor), 6 different  $(M_{ij}=M_{ji})$ . |M|=fd

$$M_{11} M_{12} M_{13}$$

$$M = M_{21} M_{22} M_{23}$$

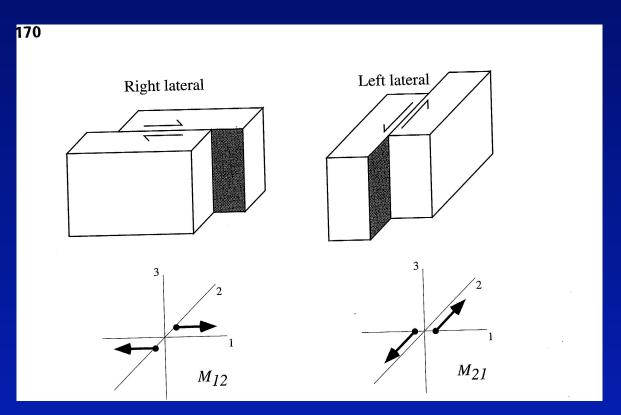
$$M_{31} M_{32} M_{33}$$

Good approximation for distant earthquakes due to a point source Larger earthquakes can be modeled as a sum of point sources



Because of ambiguity  $M_{ij}=M_{ji}$  two fault planes are consistent with a double-couple model: the primary fault plane, and the auxillary fault plane (model for both generates same far-field displacements).

Distinguishing between the two requires further (geological) information



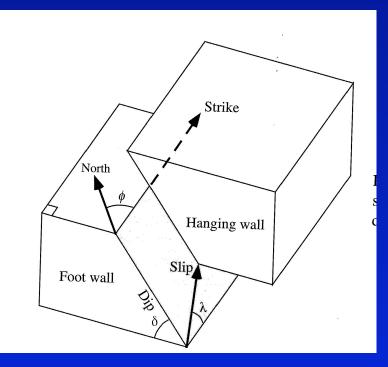
 $\mathbf{M} = \begin{bmatrix} 0 & M_0 & 0 \\ M_0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ 

Example: vertical right-lateral along x  $M_0=\mu DA$  scalar seismic moment (Nm) Description of earthquakes using moment tensors:

Parameters: strike  $\phi$ , dip  $\delta$ , rake  $\lambda$ 

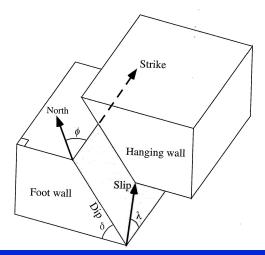
Right-lateral  $\lambda$ =180°, left-lateral  $\lambda$ =0°,  $\lambda$ =90 reverse,  $\lambda$ =-90 normal faulting

Strike, dip, rake, slip define the focal mechanism



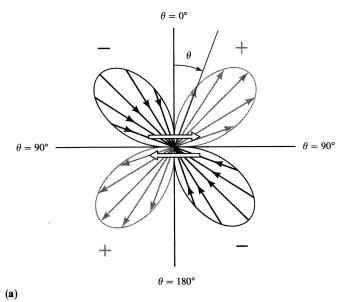
#### Description of earthquakes using moment tensors:

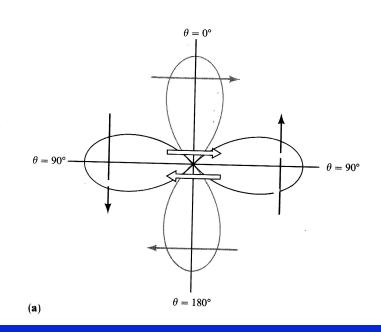
$$\begin{split} M_{11} &= -M_0(\sin\delta\,\cos\lambda\,\sin2\varphi_{\rm s} + \sin2\delta\,\sin\lambda\,\sin^2\varphi_{\rm s}), \\ M_{12} &= M_0(\sin\delta\,\cos\lambda\,\cos2\varphi_{\rm s} + 0.5\,\sin2\delta\,\sin\lambda\,\sin2\varphi_{\rm s}), \\ M_{13} &= -M_0(\cos\delta\,\cos\lambda\,\cos\varphi_{\rm s} + \cos2\delta\,\sin\lambda\,\sin\varphi_{\rm s}), \\ M_{22} &= M_0(\sin\delta\,\cos\lambda\,\sin2\varphi_{\rm s} - \sin2\delta\,\sin\lambda\,\cos^2\varphi_{\rm s}), \\ M_{23} &= -M_0(\cos\delta\,\cos\lambda\,\sin\varphi_{\rm s} - \cos2\delta\,\sin\lambda\,\cos\varphi_{\rm s}), \\ M_{33} &= M_0\,\sin2\delta\,\sin\lambda. \end{split}$$



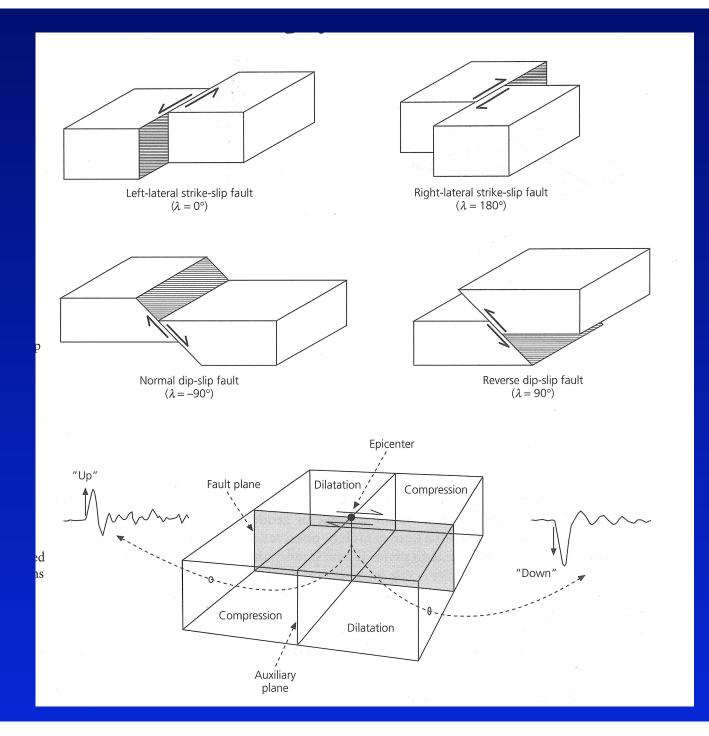
#### P-waves

#### S-waves





# Determining an earthquake's mechanism from first P motions



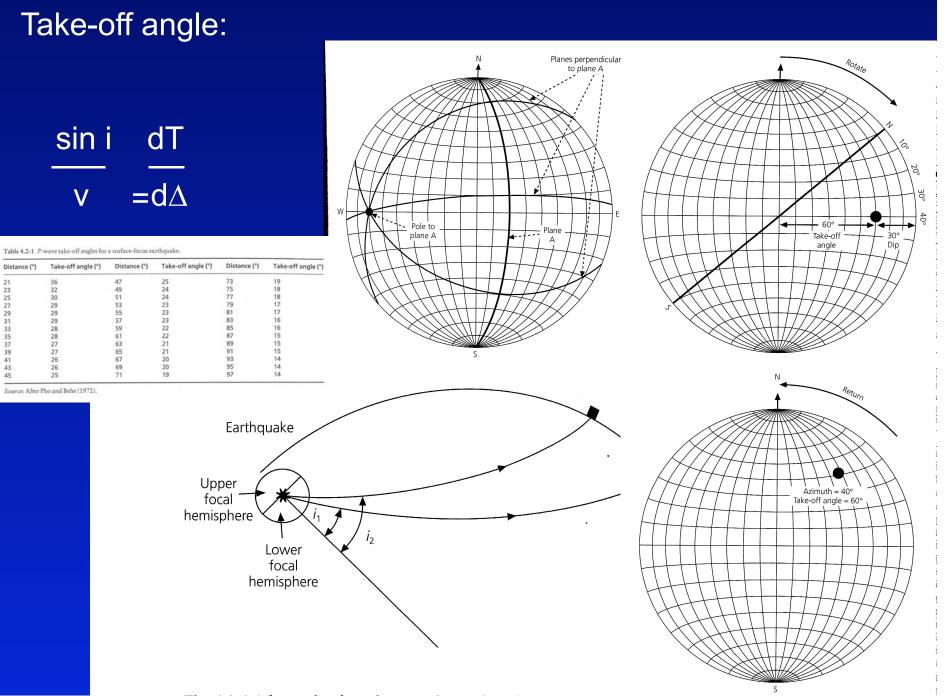
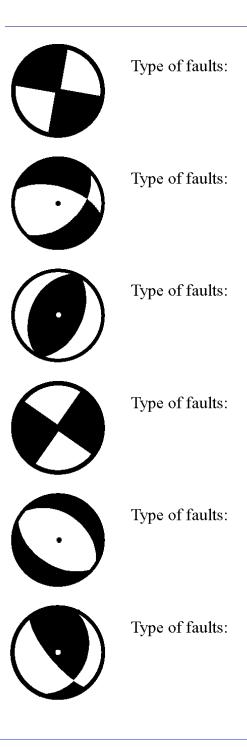
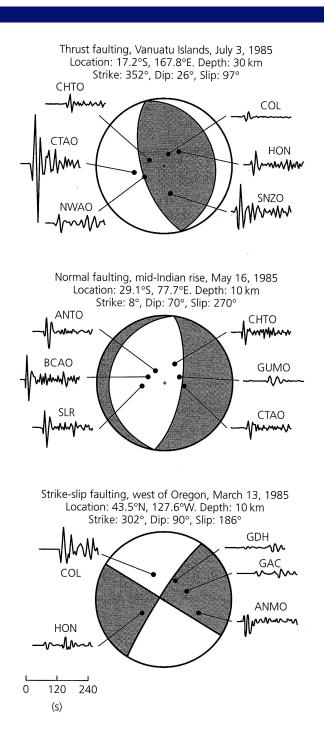


Fig. 4.2-8 The angle of incidence at the earthquake source is the a





## Earthquake focal mechanism determination from first P motion (assuming double-couple model):

- Only vertical component instruments needed
- No amplitude calibration needed
- Initial P motion easily determined (up or down)
- Up: ray left the source in compressional quadrant
- Down: ray left source in dilatational quadrant
- Plotted on focal sphere (lower hemisphere)
- Allows division of focal sphere into compressional/ dilatational quadrants
- Focal mechanism is then found from two orthogonal planes (projections on the focal sphere)

Earthquake focal mechanism determination from first P motion (assuming double-couple model):

 Focal sphere is shaded in compressional quadrants, generating 'beach ball'

- Normal faulting: white with black edges
- Reverse faulting: black with white edges
- Strike-slip: cross pattern