Earthquake Ground Motion and 3D Georgia Basin Amplification in Southwest British Columbia: Deep Juan de Fuca Plate Scenario Earthquakes

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Abstract Finite-difference modeling of 3D long-period (> 2 s) ground motions for large (Mw 6.8) scenario earthquakes is conducted to investigate effects of the Georgia basin structure on ground shaking in Greater Vancouver, British Columbia, Canada. Scenario earthquakes include deep (> 40 km) subducting Juan de Fuca (JdF) plate earthquakes, simulated in locations congruent with known seismicity. Two sets of simulations are performed for a given scenario earthquake using models with and without Georgia basin sediments. The chosen peak motion metric is the geometric mean of the two orthogonal horizontal components of motion. The ratio between predicted peak ground velocity (PGV) for the two simulations is applied here as a quantitative measure of amplification due to 3D basin structure. A total of 10 deep subducting JdF plate earthquakes are simulated within 100 km of Greater Vancouver. Simulations are calibrated using records from the 2001 Mw 6.8 Nisqually earthquake. On average, the predicted level of average PGV at stiff soil sites across Greater Vancouver for an Mw 6.8 JdF plate earthquake is 3.2 cm/s (modified Mercalli intensity IV–V). The average increase in PGV due to basin structure across Greater Vancouver is 3.1. Focusing of north-northeast-propagating surface waves by shallow (< 1 km) basin structure increases ground motion in a localized region of south Greater Vancouver; hence, scenario JdF plate earthquakes located ≥ 80 km south-southwest of Vancouver are potentially the most hazardous.

Online Material: Depth slices of 3D velocity model, peak ground velocity maps, and snapshots and videos of wave propagation.

Introduction

It is well known that earthquake waves are altered by 3D basin structure by the generation of long-period surface waves from the conversion of incident shear waves at the basin edge and/or walls (e.g., Bard and Bouchon, 1980) and by the trapping/focusing of shear waves at the basin edge (e.g., Graves et al., 1998). As an example, long-period (~ 2 s) earthquake ground motion in the soft clay basin of Mexico City during the 1985 M5 8.1 Michoacán earthquake, more than 300 km distant, was ~14 times higher (Singh et al., 1988) and lasted nearly three times longer than on firm ground nearby (Roullé and Chávez-García, 2006). Large amplification in sedimentary basins may also result from constructive interference of upward propagating shear waves and laterally propagating surfaces waves from the basin edges, known as the basin-edge effect. For example, the narrow 30 km long damage pattern in Kobe, Japan, is offset ~1 km from the fault plane of the 1995 Mw 6.9 Hyogo-ken Nanbu earthquake and is attributed to the basin-edge effect (Kawase, 1996; Pitarka et al., 1997).

Finite-difference (FD) modeling of 3D wave propagation for a variety of basins worldwide has generally shown the largest ground motions are predicted to occur near the source, above the deepest part of the basin, and near its steepest-dipping edges (e.g., Frankel and Vidale, 1992; Frankel, 1993; Olsen et al., 1995; Olsen and Archuleta, 1996). Amplification may also occur immediately behind convex basin edges or bottoms as a focusing effect (Olsen and Schuster, 1994; Olsen, 2000a). Simulations of 1D and 2D ground motion generally underpredict duration of generated surface
waves as out-of-plane wave propagation and 3D mode conversions are not accounted for. Realistic prediction of ground motion in sedimentary basins subject to the threat of future large earthquakes therefore requires 3D modeling. Ultimately, 3D basin effect simulations should be directly incorporated in the generation of probabilistic seismic-hazard maps, as was carried out for Seattle, Washington, by Frankel et al. (2007).

Advances made in FD numerical simulation in the last few decades are largely due to significant effort in predicting earthquake ground motion via 3D numerical methods of shallow earthquakes in California. For example, Graves and Pitarka (2004) extend 3D long-period (≥1 s) FD simulations to shorter periods using a stochastic approach to produce broadband synthetics, whereas Furumura et al. (2002) employ an FD method combined with a Fourier spectral method to achieve high-parallel performance for large-grid (50 million) 3D simulations. Nonuniform grid FD schemes also improve computational efficiency (e.g., Pitarka, 1999; Liu and Archuleta, 2002). A comparison of predicted ground motions of shallow California earthquakes by a variety of numerical schemes has generally demonstrated consistency, sufficient accuracy, and reliability (Aagaard et al., 2008a,b; Bielak et al., 2010; Hartzell et al., 2011). The largest discrepancies are due to differences between mesh and grid representations of the same velocity model (Bielak et al., 2010). Variability in predicted ground motion in California due to uncertainties in source or velocity models has been examined; Aagaard, Graves, Rodgers, et al. (2010) and Aagaard, Graves, Schwartz, et al. (2010) found the largest variability in predicted ground motions due to variation in rupture length (magnitude), hypocenter location, and slip distribution of the source process, whereas Hartzell et al. (2010) demonstrated that 5%-10% perturbation in a velocity model may result in up to a factor of 1.5–2.2 difference in predicted ground motions at frequencies ≤1 Hz. Other studies have explored variation in predicted ground motion due to variation of both source and velocity models or numerical schemes and source models. For example, Graves and Aagaard (2011) demonstrated that the median predicted peak ground motion of 10 FD simulations (five source models and two velocity models) of the $M_w$ 7.2 El Mayor–Cucapah earthquake is in reasonable agreement with observed measurements, whereas Hartzell et al. (2011) perform 12 simulations (four different schemes and three different source models) and find the combined model uncertainty and random variability of simulations are in the same range as variability of regional empirical ground-motion datasets. Day et al. (2008) simulated ground motions of 60 shallow earthquakes in the Los Angeles (LA) basin to complement the empirical strong-motion dataset of development of the Next Generation Attenuation of ground-motion relations. They propose a generalized predictor of long-period ground motion (geometric mean of both horizontal components) for any sedimentary basin as the depth to either a shear-wave velocity ($V_s$) of 1.0, 1.5, and 2.5 km/s (i.e., $Z_{1.0}$, $Z_{1.5}$, and $Z_{2.5}$, respectively), with preference of $Z_{1.5}$ for the LA basin.

The area of highest seismic risk in Canada is metropolitan Greater Vancouver in southwest British Columbia, with a population exceeding 2 million and critical infrastructure situated above the seismically active Cascadia subduction zone (Omur et al., 2005). In this convergent tectonic setting (Fig. 1), the oceanic Juan de Fuca (JdF) plate subducts in a northeast direction beneath the continental North America plate. Earthquakes occur in three zones: (1) the thrust fault interface between the two plates, which is currently locked and is accumulating strain to be released in future great earthquakes; (2) within the overriding North America plate, which is in compression and results in crustal earthquakes; and (3) earthquakes occur within the subducting JdF plate, mainly in response to bending of the plate at depth. The most frequent earthquakes in Greater Vancouver are JdF plate events (Halchuk and Adams, 2004); the activity rate of $M_w$ 5 JdF plate events per year is determined to be 0.0932 (one every ~10 years), and the best-estimate maximum magnitude is 7.1 (Adams and Halchuk, 2003). Figure 2 shows subducting JdF plate earthquakes are concentrated in Puget Sound, Vancouver Island, and the Queen Charlotte Fault area.
Figure 2. (a) Juan de Fuca (JdF) plate seismicity (1985–1999). Significant earthquakes (\(M_w > 6\)) are represented by stars and labeled by year. Limits of the Georgia basin regional model are shown by the solid box, and the Pacific Northwest model is shown by the dashed box. The dashed-dotted line is the international border, and the Greater Vancouver region is bounded by the dotted ellipse. The thick dashed line denotes the seismic cross-section A–A’, shown in (b) (\(M_s 2\) minimum). The color version of this figure is available only in the electronic edition.

Sound or along Georgia Strait coincident with the bend in the coastline (Rogers, 1998; Bolton, 2003). Events that occur beneath the west coast of Vancouver Island are not of concern to this study. The JdF plate is dipping at a maximum of 30° beneath Georgia Strait and Puget Sound such that the majority of events occur at 45–65 km depth and few extend to 80 km (Bolton, 2003). The largest magnitude JdF plate events tend to exhibit normal faulting (Bolton, 2003; Ristau et al., 2007). The largest JdF plate earthquakes occurred in 1949 (\(M_w 7.1\)), 1965 (\(M_w 6.5\)), and 2001 (\(M_w 6.8\)) beneath southern Puget Sound, whereas a moderate sized event (\(M_w 5.3\)) occurred in 1976 beneath Georgia Strait.

Much critical infrastructure in British Columbia, including Canada’s second busiest airport, the fourth largest tonnage port in North America, key electrical transmission corridors, and a major ferry terminal, is located on the Fraser River delta in south Greater Vancouver. This area is underlain primarily by Holocene silts and sands and Pleistocene glacial deposits that overlie an irregular Tertiary clastic sedimentary rock surface. This entire sedimentary sequence infills the Georgia basin, a northwest-oriented Late Cretaceous structural depression (Mustard, 1994; England and Bustin, 1998; Hannigan et al., 2001) that extends predominantly east across Georgia Strait to mid-Vancouver Island and south into mainland Washington (Fig. 1). The Georgia basin is one in a series of basins spanning from California to south Alaska along the Pacific margin of North America (England and Bustin, 1998), and is relatively wide and shallow (Tertiary dimensions of 130 by 70 by 5 km) in comparison to basins southward in Seattle (75 by 30 by 8 km; Frankel et al., 2007) and Los Angeles (50 by 30 by 5 km; Magistrale et al., 1996). Properties of the Late Cretaceous and Tertiary sedimentary rocks within the Georgia basin and its basement are known from seismic surveys (e.g., White and Clowes, 1984), particularly seismic tomography results of the 1998 Seismic Hazards Investigations in Puget Sound experiment (Zelt et al., 2001; Ramachandran et al., 2004; Dash et al., 2007).

Amplification of earthquake ground motion in Greater Vancouver from inevitable future large earthquakes not only depends on the 1D soil column and nonlinear response of the near-surface sediments, but also depends on the 3D structure of the Georgia basin. Realistic estimates of earthquake ground motion must account for all of these components. Previous 1D and 2D numerical modeling of earthquake response on the Fraser delta has concentrated on the effect of the relatively shallow soil layering: 1D analyses are based on vertical propagation of SH waves upward through a modeled column of the soil layering (thicknesses of investigated sites are 235 m in Molnar, 2011; 300–700 m in Onur et al., 2004; unknown in Finn et al., 2003; and 500 and 700 m in Harris et al., 1998), and the 2D analysis is based on a cross section (30 km north–south extent of 100 m depth) of the Fraser River delta (Finn et al., 2003). Predicted amplification occurs at 0.2–0.4 Hz (first higher-order modes at 1.0–1.5 Hz) due to variable accumulations of Holocene deltaic and/or Pleistocene glacial sequences. Potential amplification due to the relatively deep (upper few kilometers) Georgia basin sedimentary structure is virtually unknown; Tertiary/Late Cretaceous basin sediments are considered as basement in the previous 1D and 2D numerical analyses, and empirical amplification at long periods (\(\geq 0.5\) Hz) is not resolved by the current strong-motion database, which consists of low-level (\(\leq 5\%\)) earthquake recordings of primarily short (~30 s) duration. Amplification observed from these low-level earthquake recordings (0.5 Hz minimum) is 4–11 times that of hard rock at 1.5–4.0 Hz (Cassidy and Rogers, 1999, 2004). Hence, this study uses 3D numerical modeling to address the gap in knowledge of potential long-period amplification due to the relatively deep Georgia basin in southwest British Columbia. In Greater Vancouver, long-period amplification is of concern; for example, over 700 commercial and residential buildings are 12 stories or taller, which are likely to have low-resonance frequencies (\(\leq 0.5\) Hz).

Sedimentary basins in subduction zone settings similar to the Georgia basin include those in Japan, Taiwan, and Mexico. Iwaki and Iwata (2010) perform long-period (> 3 s) FD simulation of an \(M_{WMA} 6.5\) aftershock to assess applicability of a 3D Osaka basin model. The simulation reproduces the observed peak motion at many stations, but...
overestimates at some stations, as well as reproduces the empirical horizontal-to-vertical spectral ratio peak period within 1 s at many stations. The Yufutsu basin in Northern Japan generally deepens west to east, with an internal sub-basin that deepens east to west; Aoi et al. (2008) perform a series of long-period (>3 s) FD simulations of the 2003 $M_w$ 8.3 Tokachi-Oki earthquake (42 km depth) with or without particular basin layers and demonstrate that the sub-basin is effective in amplifying and extending long-period motions causing significant damage to oil tanks due to sloshing. Long-period (>1 s) FD simulations of a small earthquake close to the Taipei basin, Taiwan, by Miksat et al. (2010) demonstrates amplification is a factor of 4 (compared to hard rock conditions) due to basin structure; maximum amplification is a factor of 8 once amplification due to the low-velocity Songshan formation is included, which is in fair agreement with observed amplification greater than a factor of 5. Lee et al. (2008) demonstrate that the low-velocity Songshan formation dominates the amplification and wave propagation behavior (≤3 Hz resolution) for a simple point source at 1 km depth in a shallow Taipei basin model. High-resolution (20 m grid) spectral element numerical simulations, which include the mountainous topography (≤3 km above sea level) that surrounds the Taipei basin, demonstrate that peak ground motions increase up to 50% in the basin for deep scenario events due to scattering of body waves by the enclosing mountains, which then propagate as surface waves into the basin, whereas for shallow earthquakes, topography scatters surfaces waves and reduces predicted peak motions (Lee et al., 2009). Furumura and Singh (2002) perform spectral-element simulations of both a shallow (17 km) $M_w$ 7.3 interplate earthquake along the Mexican subduction zone and a deep (40 km) $M_w$ 7.5 inslab normal-faulting earthquake in the subducted Cocos plate. The shallow interplate event causes very large ground motions (frequency bandwidth of 0.2–4 Hz) along the path from the coast to the Mexican interior due to interference of multiple crustal arrivals ($L_g$ phase), whereas ground motions for the deeper inslab normal-faulting event demonstrate simple attenuation with increasing distance, that is, the $L_g$ phase is too small.

This paper presents FD simulations of long-period (>2 s) ground motions computed for scenario deep JdF plate earthquakes in southwest British Columbia in a regional 3D velocity model of the Georgia basin, Molnar et al. (2014) deals with shallow (5 km) crustal North America plate scenario earthquakes (Molnar et al., 2014). This research provides the first detailed investigation of 3D earthquake ground motion for a sedimentary basin in Canada. The main objective here is to examine the effect of the 3D Georgia basin structure on predicted ground shaking across Greater Vancouver from large ($M_w$ 6.8) scenario earthquakes. The scenario earthquakes considered in this paper include deep (42–55 km) subducting JdF plate events with a seismic radiation pattern equivalent to that of the normal-faulting 2001 $M_w$ 6.8 Nisqually, Washington, earthquake. Scenario earthquakes are simulated in different epicenter locations in the Georgia basin region, congruent with known seismicity and within 100 km of Vancouver, to investigate variation in the strength of predicted ground motions and 3D basin effects. The chosen peak ground velocity (PGV) metric here is geometric mean of the two orthogonal horizontal components, calculated as $\max_{t}(\sqrt{v_{EW}(t) \times v_{NS}(t)})$, in which $v(t)$ represents a synthetic horizontal velocity waveform, EW represents east–west component and NS represents north–south component. The preferred intensity measure of the American Society of Civil Engineers (ASCE) has changed from the geometric mean value (ASCE, 2006) to the maximum rotated value (ASCE, 2010) of the two orthogonal horizontal components. Peak motion values based on the square-root sum of squares of both horizontal and all three components of motion, termed 2DrssPGV and 3DrssPGV, respectively, are also provided here as an approximation of maximum rotated PGV (NEHRP Consultants Joint Venture, 2011). Amplification due to basin structure is evaluated as the ratio of peak motion from simulations of the same scenario earthquake in 3D basin and nonbasin structure models, as performed for the LA basin by Olsen (2000b). In order to conduct this research, the Georgia basin 3D structure model is revised with recent geological and geophysical information and calibrated by simulating the Nisqually earthquake and comparing the synthetic results to recordings. Limitations of this work include: (1) uncertainty in physical-structure and source-rupture models, (2) omission of low-velocity material (e.g., water and up to 300 m of Holocene sediments) and surface topography in the physical-structure models, and (3) inability to resolve frequencies > 0.5 Hz. Nonetheless, the work presented here (and in Molner et al., 2014) represents an important first step toward quantifying the effect of the 3D sedimentary Georgia basin structure on earthquake ground motion in southwest British Columbia.

### Physical-Structure Models

The base elastic 3D model is extracted from the Stephenson (2007) Pacific Northwest 3D velocity model that was produced for simulations of $M_w$ 9 Cascadia megathrust events (Olsen et al., 2008). Two different sizes of physical-structure models are used; a Pacific Northwest model that spans from northwest Washington to southwest British Columbia (dashed box in Fig. 2) is used for simulation of the Nisqually earthquake at > 150 km from Greater Vancouver, and a smaller regional model (solid box in Fig. 2) is used for simulations of scenario JdF plate earthquakes within 100 km of Greater Vancouver. Table 1 provides details of the Pacific Northwest and regional velocity models.

The physical-structure model is described fully in Stephenson (2007) and only a brief overview is given here. The physical model is represented by six geologic units (continental basin sediments, crust, and mantle; and oceanic sediments, crust, and mantle) characterized by $V_p$, $V_s$, and density. The thickness of the oceanic crust was set to 5 km. The 3D sedimentary basin structure in the Georgia basin
region is primarily constrained by the tomographic $V_P$ model (1 km resolution) of Ramachandran et al. (2004, 2006). The $V_P/V_S$ ratio for Quaternary basin sediments varies from 2.5 at the surface to 2.2 at 1 km depth. Tertiary sediments are set to a $V_P/V_S$ ratio of 2, and their base is taken as the 4.5 km/s $V_P$ contour (Ramachandran et al., 2006). Densities are derived from the $V_P$ model using the Nafe–Drake relation (Ludwig et al., 1970). Surface topography is not included. The minimum $V_S$ is set to 625 m/s for computational feasibility (Olsen et al., 2008). In south Greater Vancouver, up to 300 m of Holocene deltaic sediments of the Fraser River are effectively ignored, that is, are represented by a $V_S$ of 625 m/s. The surface of the 3D basin model therefore represents overconsolidated Pleistocene glacial sediments or stiff soil sites. This is a significant limitation to modeling of the potential earthquake ground motion here, and the overall amplitude and duration of simulated ground motions in the Georgia basin are likely biased. For example, if >200 m of lower-velocity material is present, applicable to the Fraser River delta in south Greater Vancouver, amplification will be increased by a factor of ~2 from that presented here (Molnar, 2011).

For the FD simulations carried out in this paper (in Molner et al., 2014), the upper 1 km of the base elastic 3D model is updated in the Georgia basin region of southwest British Columbia. Regions with thick accumulations of unconsolidated Pleistocene and younger sediments known from high-resolution shallow seismic data (Hamilton, 1991; Mosher and Hamilton, 1998) are not resolved in regional tomographic $V_P$ models (Lowe et al., 2003). In the base elastic 3D model, a northeast-trending velocity contrast occurs beneath Greater Vancouver, which is not supported by geological and structural information, but rather results from extrapolation of the 1 km gridded $V_P$ model of Ramachandran et al. (2006) to the surface. When the base elastic 3D model is used in FD simulations of the Nisqually earthquake, good agreement is obtained between synthetic and empirical waveforms in the Seattle basin region (Molnar et al., 2010), because significant effort had gone into validating the 3D model (Frankel and Stephenson, 2000; Hartzell et al., 2002; Pitarka et al., 2004; Frankel et al., 2007, 2009). However, synthetic waveforms overpredict Nisqually waveform amplitudes in the Georgia basin region by a factor of 2.1 (Molnar et al., 2010). Therefore, in order to update $V_P$ in the upper 1 km of the base elastic 3D model in the Georgia basin region for the modeling work conducted here, all nonconfidential government geological and geophysical datasets, as well as the higher-resolution (600 m gridded) tomographic regional model of Dash et al. (2007), were collected, converted to $V_P$ estimates (if required), and merged (details in Molnar, 2011). The $V_P/V_S$ ratio is set to 2 for $V_P \leq$ 5.5 km/s in the updated 3D basin model; the base of the Georgia basin is composed of Late Cretaceous Nanaimo Group rocks, inferred as the 5.5–6.0 km/s $V_P$ surface in regional tomographic $V_P$ models (Zelt et al., 2001; Ramachandran et al., 2004, 2006; Dash et al., 2007). This higher $V_P$ limit for the $V_P/V_S$ ratio of 2 effectively causes low $V_S$ values to extend to greater depths in the updated model. Otherwise, relationships of $V_P$ with $V_S$ remain unchanged. Densities are derived from the $V_P$ model using the Nafe–Drake relation (Ludwig et al., 1970) and are in agreement with the 3D Georgia basin density model of Lowe et al., (2003).

A nonbasin 3D model is also generated from the updated basin model by setting the minimum $V_P$ to 5.5 km/s, effectively replacing basin sediments with inferred basement. Structural studies in this region have shown that basement units surrounding the Late Cretaceous Georgia basin sediments correspond to $V_P$ of ~5.5–6.0 km/s in the upper 2 km and ~6.4–6.75 km/s at deeper depths (White and Clowes, 1984; Zelt et al., 2001; Ramachandran et al., 2004, 2006; Dash et al., 2007). Expected reduction in seismic velocity of basement rock units in southwest British Columbia likely occurs in the upper tens of meters, which is not resolved by the chosen 250 m gridded velocity model. Therefore, the nonbasin velocity model is based on the typical 1D velocity profile for rock sites in southwest British Columbia. Figure 3 compares the 500 m depth surface and 8 km deep cross sections of the updated basin and nonbasin regional models (see Fig. S1 for depth surfaces to 7 km, available in the electronic supplement to this paper). The maximum depth of the Georgia basin is 6.5 km at its southeast extent; hence, the basin and nonbasin models are identical below 6.5 km depth. Simulations using the nonbasin model represent shaking due to source characteristics and background regional structure. For the same scenario earthquake, the ratio of peak motions predicted using the basin and nonbasin models provide a quantitative measure of 3D Georgia basin effects. The advantage of
calculating basin/nonbasin ratios of peak motion noted by Olsen (2000b) is the removal of geometrical spreading effects included in the basin response and the nonbasin reference value for a given site, with the disadvantage that artifacts occur in maps of basin/nonbasin peak motion due to singularities in the rupture pattern.

**Finite-Difference Scheme**

The 3D elastic equations of motion are solved here using the FD scheme of Olsen (1994) with fourth-order accuracy in space and second-order accuracy in time. This scheme has been verified against other FD and finite-element methods for reference (1D) benchmarks as well as realistic basin (3D) shapes (e.g., Day et al., 2008; Bielak et al., 2010). The physical model is represented by a uniform cubic mesh discretized with a spacing equivalent to five nodes per minimum shear wavelength (e.g., Levander, 1988; Moczo et al., 2000), which limits the maximum resolvable frequency. In this work, the uniform grid size of the physical model is 250 m, with a minimum $V_s$ of 625 m/s, such that the maximum resolvable frequency is 0.5 Hz (2 s period). Viscoelasticity is incorporated independently for P and S waves using a coarse-grained implementation of the memory variables (Day, 1998; Day and Bradley, 2001). Generally, the most important parameters for ground-motion prediction are $V_S$ and $Q_S$, which govern shear and surface-wave arrivals associated with the strongest ground motions (Brocher, 2007). Various $Q$ relations were tested (Olsen, 2003; Brocher, 2008; Frankel et al., 2009) but cause minimal variation to the resulting low-frequency ground motions. The $Q$ relations of Frankel et al. (2009) for stiff sediments in the Pacific Northwest are the most geologically reasonable and are assigned here: for $V_S < 1000$ m/s, $Q_S = 0.1643 \times V_S - 14$; for $V_S > 1000$ m/s, $Q_S = 0.15 \times V_S$; and $Q_P = 2 \times Q_S$. Overall, $Q_S$ increases from 89 at the surface to 723 at 60 km depth in the updated 3D basin model.

Table 1 provides further details of the modeling parameters. The FD code was compiled on the Minerva IBM Nighthawk-2 SP supercomputer at the University of Victoria. The Nisqually earthquake is simulated using arithmetic averaging (Olsen, 1994; version 2.5.1) and absorbing boundary conditions (Clayton and Engquist, 1977) including a zone of highly attenuative material (Cerjan et al., 1985) in the Pacific Northwest model (2.6 \times 10^8 grid nodes). For this model, the use of the generally higher-accuracy harmonic averaging is inhibited by the presence of water in the model with $V_S = 0$. All other deep JdF plate events are simulated within 100 km of Greater Vancouver using harmonic averaging (Olsen, 1994; version 2.6.4) and more efficient perfectly matched absorbing layers boundary conditions (Collino and Tsogka, 2001; Marcinkowski and Olsen, 2003) in the Georgia basin region model (1.0 \times 10^8 grid nodes). The seismic source is implemented in the FD grid by adding $-M_{ij}(t)/V$ to $S_{ij}(t)$, in which $M_{ij}(t)$ is the $ij$th component of the moment tensor for the earthquake, $V = dx^3$ is the cell volume, and $S_{ij}(t)$ is the $ij$th component of the stress tensor on the fault at time $t$ (Olsen, 2000b).

**Earthquake Source Model**

The most recent and best-constrained large magnitude earthquake in the Pacific Northwest is the 2001 $M_w$ 6.8 Nisqually earthquake. Of the 12 earthquakes recorded since
the 1960s by the strong-motion network in southwest British Columbia (Cassidy et al., 2008), the Nisqually earthquake generated the highest-quality dataset with 96 recordings of 15–90 s recording length and sufficient signal-to-noise ratio. From seven studies of the Nisqually earthquake’s source parameters (Bustin et al., 2004), the earthquake is a normal-faulting event that ruptured at 49–55 km depth along a north-striking, steeply east-dipping fault (or south-striking shallow west-dipping fault) and released a total seismic moment of 1.4–2.0 × 10^{19} N·m. Kao et al. (2008) applied a source-scanning algorithm to local seismic waveforms and showed unambiguously that rupture occurred along the north-striking steeply east-dipping fault plane. The imaged source process occurs in two pulses, with a slightly stronger second pulse and a total duration of ~6–7 s. Rupture characteristics of other large JdF plate events in 1949 and 1965 are also best represented by a double-pulse release of seismic moment (Ichinose et al., 2004, 2006; Wiest et al., 2007), with a duration of 12–22 s for the larger (M_w 7.1) 1949 event (Wiest et al., 2007). Hence, a source model based on the Nisqually earthquake rupture is considered to best represent rupture for large JdF plate earthquakes and is used here for all 10 scenarios.

Previous FD simulations of the Nisqually earthquake, including comparison with recordings, for the Seattle basin region were carried out by Pitarka et al. (2004) and Frankel et al. (2007, 2009). Table 2 provides details of the Nisqually earthquake source model of Pitarka et al. (2004), used here for the Nisqually earthquake and all 10 scenario earthquake simulations. This model is also used by Frankel et al. (2009), whereas Frankel et al. (2007) used a slightly longer duration of 1.7 s between point sources. Variations of the Nisqually earthquake source model were tested for this study: a 50% reduction or 20% increase in PGV (single horizontal component) was observed when the source model was adjusted to release the total seismic moment in a single 8.5 s pulse or in two consecutive 4.0 s pulses, respectively, but negligible PGV variation was observed when the two pulses were separated by 1.5 s or 1.7 s (Molnar et al., 2008).

Accuracy of the Simulations

Finite-difference simulation of the Nisqually earthquake is performed here, using the updated 3D Pacific Northwest basin model to calibrate synthetic results with recordings to more accurately predict long-period ground motions for large JdF plate scenario earthquakes. Figure 4 compares empirical and synthetic waveforms at 18 selected strong-motion sites in the Seattle basin region (generally similar sites chosen by Pitarka et al., 2004, and Frankel et al., 2007, 2009). All empirical waveforms are synchronized to 10:54:26 PST (time zero), the origin time of the Nisqually earthquake is 6.78 s later at 10:54:32.78 PST, and the synthetics have been shifted to 10:54:33.75 PST (i.e., synthetic S waves arrive ~1 s later than empirical). The qualitative agreement observed between waveforms here is similar to that shown in Pitarka et al. (2004) and Frankel et al. (2007, 2009). The deep Seattle basin structure generates more complex and longer duration synthetic waveforms than at sites outside of the basin. Significant long period ground motions are generated at the south edge of the Seattle basin (strong velocity contrast), in agreement with observed stronger amplification for earthquakes from the south-southwest (Frankel et al., 2009) and coincident with the zone of chimney damage from the Nisqually earthquake (Stephenson et al., 2006).

Figure 5 presents waveform comparisons for 16 selected weak- and strong-motion sites in the Georgia basin region. Of the 16 sites, two are strong-motion stations in northeast Washington, four are weak-motion seismograph stations of the Canadian National Seismograph Network located on rock sites surrounding the Georgia basin, and the remaining 10 stations are strong-motion stations of the Geological Survey of Canada and British Columbia Hydro located in Greater Vancouver, four of which are located on low-velocity Holocene sediments of the Fraser River delta (not included in the 3D basin model). The duration of earthquake recordings at rock sites is generally <35 s; longer duration records of 50–97 s are obtained at the soil sites. These strong-motion instruments operate on batteries with internal clocks that drift over time, such that accurate timing is not obtained. Each empirical waveform is shifted based on best visual fit with the corresponding synthetic waveform, the average offset is ~55 s, similar to the time of the S-wave arrival at weak-motion seismograph sites with accurate timing (i.e., ~50 s at SNB and ~60 s at HNB).

Ground motions in the Georgia basin region from the M_w 6.8 Nisqually earthquake are significantly lower than in the Seattle basin region, as the deep earthquake is >150 km distant. Recordings at stations south of the Georgia basin (ERW, PGC, SBES, and SNB) generally show larger east–west than north–south arrivals (Fig. 5), in agreement with predictions, but overall the predicted amplitudes are larger. For stations in the Georgia basin (ANN, ARN, EBT, ING, KID, and RHA), predicted PGV is associated with later arriving surface waves, east–west motion is larger than north–south motion, and there is generally good agreement with recordings. Good peak agreement occurs because empirical PGV at soil sites (ANN, ARN, KID, and RHA) is similar to the PGV of later arriving surface waves in the synthetic waveforms.

Following Frankel et al. (2009), Figure 6 compares empirical and predicted PGVs for all 36 selected recording sites in Washington and British Columbia. All waveforms are
band-pass filtered between 0.01 and 0.5 Hz. The simulations conducted in this study generally overpredict empirical PGVs in the Seattle basin region (PGV > 1 cm/s) but capture the trend of the data. For the 18 sites in the Seattle basin region, the bias in PGV is 0.44 natural log units (factor of 1.5; synthetics larger than recorded) with one standard deviation of 0.35 natural log units (factor of 1.4). In comparison, goodness-of-fit factors in peak motion within the Seattle basin region obtained by Pitarka et al. (2004) are similar to this study (Molnar, 2011). Frankel et al. (2009) use the same physical-structure and source-rupture models as used here to simulate the Nisqually earthquake but use a nonuniform FD scheme. They report a PGV bias of 0.096 natural log units (factor of 1.1) with one standard deviation of 0.27 natural log units (factor of 1.3). In comparison, the 2DgmPGV bias is then 0.30 natural log units (factor of 1.3) and one standard deviation of 0.28 natural log units (factor of 1.3).

Figure 6 shows larger variation is obtained between empirical and predicted PGVs in the Georgia basin region (PGV < 1 cm/s). The average factor of PGV overprediction in the Georgia basin region is 2.1 for the Stephenson (2007) velocity model (6a) and 1.6 for the updated velocity model (6b); incorporation of high-resolution shallow seismic data in the basin velocity model results in an average 24% reduction in bias of predicted PGV.

Simulation of the $M_w$ 6.8 Nisqually earthquake and comparison with recordings demonstrates good agreement in amplitude and phase of first arrival $S$ waves at stations within 100 km of the source (Seattle basin region, Fig. 4), providing confidence in the Nisqually source model. Overall, general agreement of the waveforms in the Seattle basin region is
Figure 5. Comparison of 0.01–0.5 Hz synthetic (light lines) and empirical (black lines) long-period Nisqually earthquake waveforms at 16 sites in the Georgia basin region, spanning north Washington to southwest British Columbia. The color version of this figure is available only in the electronic edition.

Figure 6. Comparison of predicted and empirical PGVs for the Nisqually earthquake from 3D FD simulations using (a) the Stephenson (2007) velocity model and (b) the updated basin velocity model. Open squares are based on the largest 0.01–0.5 Hz peak velocity from the two horizontal components for a given station; filled squares are based on the geometric mean of the two horizontal components at a given site.
Scenario Earthquakes

The goal here is to quantify the 3D Georgia basin effect on long-period ground shaking in Greater Vancouver for realistic scenarios of $M_w$ 6.8 JdF plate earthquakes. Figure 7 shows the epicenter locations of 10 scenario JdF plate earthquakes considered here, chosen in a 30–40 km grid-spacing spanning the Georgia basin region congruent with known seismicity (Fig. 2). At each scenario earthquake location (Table 3), the Nisqually earthquake source model is initiated near the top of the oceanic crust which subducts northeast beneath Greater Vancouver; hence, the deepest earthquakes occur toward the northeast. The maximum source depth is constrained to 55 km by the maximum 60 km depth of the regional velocity structure models (Table 1). The most realistic scenarios are those along the extent of the Georgia Strait for the chosen magnitude and depth limitations of the model (scenarios 1, 2, 6, 9, and 10); ground motions are likely biased upward for scenarios furthest northeast (scenarios 3 and 4).

Ground-Motion Modeling

Figure 8 shows time snapshots at 5 s intervals of the east–west component PGV for the 70 s simulation of deep JdF plate earthquakes with epicenter locations 40 km west (scenario 2), 50 km south (scenario 6), and 95 km south (scenario 9) of Greater Vancouver. For time snapshots of all three components of motion, see Figure S2 (available in the electronic supplement); the largest motion occurs on the east–west component due to rupture of the north-striking steeply east-dipping normal-faulting source model. Videos of simulations for these three selected scenario earthquakes are available in the electronic supplement. For all 10 scenario earthquakes, surface ground shaking does not occur until 10–15 s into the simulations due to the 42–55 km source depths. The double-pulse nature of the rupture is evident at 20–25 s as two circular wavefronts radiating outward from the scenario epicenter location. The symmetry of the rupture is distorted as waves enter the Georgia basin, that is, wave motion is slowed down by the presence of lower-velocity basin sediments. From 30 s onward, basin surface waves are generated, primarily aligned in a northwest–southeast sense along the basin axis, and are sustained within the basin. The largest amplitude surface waves are generated offshore of Greater Vancouver, toward the northwest and south, coincident with steep edges in the upper 1 km of the basin model. The largest amplitude surface waves arriving in Greater Vancouver occurs at ~50 s for scenario 8, 100 km southwest of Vancouver from focusing (constructive interference) as they propagate north across the city. Larger amplitude surface waves in Greater Vancouver are not produced by any of the other nine simulated deep JdF plate earthquakes, although multiple cycles of slightly lower-amplitude surface waves at ≥60 s are generated in Greater Vancouver for scenario 9, 95 km south of the city.
Table 4 lists the maximum PGV (three different metrics) within the Georgia basin and Greater Vancouver regions for each scenario earthquake, as well as the average maximum PGV for all 10 scenario earthquakes for each region. The 2DrssPGV values are generally higher than the preferred geometric mean PGV (2DgmPGV) values, as expected, and are similar to 3DrssPGV values because the vertical component motion is here generally of smaller or similar amplitude to horizontal motion here. Figure 9 shows PGV maps (2DgmPGV metric) for all 10 scenarios; panel layout corresponds to the spatial distribution of scenario earthquake epicenter locations. Figures S3 and S4, available in the electronic supplement to this paper, show PGV maps of each individual component of motion and 3DrssPGV, respectively, for all 10 scenarios. Generally, the highest ground motions are coincident with the lowest velocity sediments in the upper 1 km of the model (see Figs. 1 and S1a in the supplement), although the level and spatial extent of ground shaking is unique to each scenario. The range in predicted maximum PGV in the Georgia basin region is 4.8 to 9.1 cm/s, modified Mercalli intensity (MMI) of V–VI (Wor- den et al., 2012). Maximum PGV in Greater Vancouver ranges from 2.6 to 4.3 cm/s, corresponding to MMI IV–V. For context, the $M_{w}$ 6.8 Nisqually earthquake produced long-period shaking levels ≤5 cm/s in the Seattle basin (Fig. 4) and resulted in U.S. $2 billion worth of damage in Washington.

Basin Amplification

Figure 10 displays east–west component waveforms at 20 locations along a 100 km long north–south profile (5 km spacing) through Greater Vancouver for 8 selected scenario events simulated in both the basin and nonbasin models. The bottom panels display the cross-sectional velocity structure for each model to 10 km depth (maximum model grid depth is 60 km). Figure S5, available in the electronic supplement, compares basin and nonbasin waveforms for the north–south and vertical components. For each scenario, predicted amplitudes and duration of shaking is increased within the basin (at distances of ~25–75 km) in comparison to nonbasin model simulated waveforms. All waveforms display two early S-wave arrivals due to the rupture character of the source. The amplitude of these early S-wave arrivals is largest in Greater Vancouver for the deep JdF plate earthquake 25 km east of the city (scenario 4). The largest later-arriving surface waves in Greater Vancouver occur for the scenario 100 km southwest of Greater Vancouver (scenario 8). Figure 10 clearly shows the predicted variation in shaking level and duration for the 10 scenarios of deep JdF plate earthquakes within the Georgia basin region.

Figure 11 shows basin amplification maps (ratio of 2DgmPGV between basin and nonbasin simulations) for the 10 scenario JdF plate earthquakes. As an example, the east–west component waveform at a selected location within Greater Vancouver is also shown in Figure 11 for the basin and nonbasin model simulations of each scenario earthquake. The presence of the northwest-oriented Georgia basin is readily apparent and is associated with amplification factors ≥2.5. The highest basin amplification (up to a factor of 11) generally occurs near each earthquake epicenter but is generally coincident with the lowest-velocity Georgia basin sediments in the upper 1 km (see Figs. 3 and S1a in the supplement). In Greater Vancouver, the highest ground motions are associated with the scenario earthquake 25 km east of the city (scenario 4), but the highest basin amplification
(factor of > 4.5) is associated with scenario earthquakes located ≥80 km south-southwest of the city (scenarios 8, 9, and 10) due to the occurrence of later-arriving surface waves in basin model waveforms. Basin amplification factors based on the 3DrssPGV metric are listed in Table 4 and displayed in Figure S6 (available in the electronic supplement). Generally, basin amplification factors increase as PGV values decrease; the 3DrssPGV metric determines the highest PGV values and the lowest, and most stable, basin amplification factors.

Discussion

A set of 10 scenario $M_w$ 6.8 JdF plate earthquakes are simulated in the Georgia basin and nonbasin structure models to predict long-period ground motions in Greater Vancouver. Figure 12 presents maps of the average PGV and basin amplification of all 10 scenario earthquakes. These maps are considered to provide an estimate of the average peak motion and basin amplification related to a deep JdF plate earthquake within 100 km of Greater Vancouver. The presence of the Georgia basin significantly increases the level of predicted long-period ground motions. For the Georgia basin region as a whole, the average maximum PGV is 4.6 cm/s, related to an MMI V. The average maximum basin amplification is a factor of 4.5. For comparison, Olsen (2000b) determined the average maximum basin amplification of the LA basin for nine scenario events to be 4.2.

More importantly, in the onshore Greater Vancouver region, the average maximum peak motion is 3.2 cm/s. Therefore, on average, the predicted intensity of shaking at stiff soil sites in Greater Vancouver for an $M_w$ 6.8 JdF plate
earthquake corresponds to MMI IV–V. The basin structure model does not include soft sediments \((V_S < 625 \text{ m/s})\) or surface topography, which may also amplify ground shaking. For reference, PGV at stiff soil sites in the Seattle basin region correspond to MMI IV from the \(M_w 6.8\) Nisqually earthquake, which caused U.S. $2 billion worth of damage in Washington. The average maximum increase in peak motion due to basin structure in south Greater Vancouver is a factor of 3.1.

The proposed predictor variable for basin amplification is the depth to either a \(V_S\) of 1.0 \((Z_{1.0})\), 1.5 \((Z_{1.5})\), or 2.5 \((Z_{2.5})\) km/s, in which \(Z_{1.5}\) is preferred for the LA basin \((\text{Day et al., 2008})\). To investigate which proposed predictor variable may be applicable to the Georgia basin, the overall average basin amplification map is compared with isodepth contours of 1.0, 1.5, and 2.5 km/s sediments in the basin structure model in Figure 13. The area of highest basin amplification (3–4) is primarily associated with the lowest velocity sediments in the upper 1 km, that is, \(Z_{1.0}\) at 250 m depth and \(Z_{1.5}\) at 500 m depth. An appropriate measure of basin amplification for the Georgia basin appears to be \(Z_{1.0}\) or \(Z_{1.5}\), but not \(Z_{2.5}\). Hence, ground-motion prediction equations that utilize \(Z_{2.5}\) as the basin sediment-thickness correction term should not be used for sites within the Georgia basin. Comparisons with a short-period site correction term (e.g., \(V_{S30}\)) are not possible here due to the long-period nature of the modeling, that is, 250 m uniform grid and minimum \(V_S\) of 625 m/s.

### Conclusions

To assess the effects of the 3D Georgia basin structure on long-period (>2 s) ground motion due to large earthquakes within 100 km of Greater Vancouver, numerical 3D FD modeling of viscoelastic wave propagation is carried out. This research provides the first detailed investigation of 3D earthquake ground motion for a sedimentary basin in Canada. Shorter period ground motions are not resolved, limited by the grid spacing and minimum \(V_S\) chosen for the 3D basin model according to a \(\geq 5\) node per minimum shear wavelength rule-of-thumb commonly used for fourth-order FD schemes. Overall the work presented here (and in \text{Molnar et al., 2014}) represents an important step toward quantifying the effect of the Georgia basin on earthquake ground motion in southwest British Columbia.

### Accuracy of the 3D FD simulations

The accuracy of the 3D FD simulations is evaluated here by comparing predicted and empirical waveforms of the 2001 \(M_w 6.8\) Nisqually earthquake; the only large goodness empirical dataset available for the Georgia basin region. General agreement in amplitude and phase of first
Figure 10. Synthetic basin and nonbasin east–west component waveforms for eight selected scenario earthquakes along the north–south profile shown in Figure 7. The bottom panels shows the corresponding vertical cross sections of the basin and nonbasin models (contours of $V_p$, km/s are labeled) to 10 km depth.
arrival S waves is obtained at stations in the Seattle basin within 100 km of the source; the Nisqually earthquake source-rupture model is relatively well determined from previous 3D FD simulation studies (Pitarka et al., 2004; Frankel et al., 2007, 2009). In this near-source region, estimates of PGV (0.2–0.4 Hz bandwidth) are biased by a factor of 1.3 (this study) and 1.1 (Frankel et al., 2009) for the same physical-structure and source-rupture models; Frankel et al. (2009) obtain slightly better agreement by using a nonuniform FD scheme, that is, inclusion of smaller scale structure toward surface increases the accuracy of predicted long-period ground motions. For the Georgia basin region, the bias between predicted and empirical PGV is a factor of 2.1, which is reduced to a factor of 1.6 when the base Pacific Northwest velocity model is updated here with higher-resolution shallow (<1 km) geologic and geophysical datasets. Improvement in predicted low-frequency ground motions is negligible for a variety of physically reasonable $Q$ relations for the lowest velocity sediments in the basin model. Overall, general agreement of waveforms in the near-source region is achieved and provides confidence in the use of the Nisqually earthquake source model to simulate large subducting JdF plate scenario earthquakes in the Georgia basin region.

A total of 10 scenario earthquakes within the subducting JdF plate (42–55 km depth) are simulated with hypocenters in realistic locations based on known seismicity. All simulated earthquakes are characterized by the same source

Figure 11. Maps of basin amplification for all 10 scenario earthquakes; stars show epicenter locations, and the coastline and international border are shown by black lines. Numbers in the upper right of each panel correspond to the maximum basin amplification factor within the Georgia basin (map area shown north of $5.38 \times 10^6$ m) and Greater Vancouver (dashed rectangle) regions. A synthetic east–west component waveform is shown in the upper right of each panel for the basin (upper waveform) and nonbasin (lower waveform) model simulations corresponding to a location within Greater Vancouver (small square). The color version of this figure is available only in the electronic edition.
Figure 12. (a) Average PGV and (b) basin amplification for all 10 scenario earthquakes. The coastline and international border are shown by black lines. Greater Vancouver is outlined by the dashed rectangle. The color version of this figure is available only in the electronic edition.

Figure 13. Average basin amplification compared to $Z_{1.0}$, $Z_{1.5}$, and $Z_{2.5}$ isodepth contours in the upper 2 km of the basin model. The coastline and international border are shown by thin black lines. The color version of this figure is available only in the electronic edition.
process of the Nisqually earthquake. Nonetheless, the FD simulations presented here provide significant insight to the expected amplification in ground shaking due to 3D basin structure. For all simulations, some general effects are observed consistently when Georgia basin sediments (625 m/s ≤ V_p < 5.5 km/s) are included in the 3D structure model. The symmetry of the seismic radiation pattern is distorted, and the area of higher ground motions is increased. Surface waves are generated in the southeast and northwest parts of the basin coincident with steep basin edges in the upper 1 km of the model. The average maximum peak ground motion for an M_w 6.8 JdF plate earthquake in the Georgia basin model is 4.6 cm/s (MMI V), and the average maximum basin amplification is 4.5; for the Greater Vancouver region, the average maximum PGV and basin amplification is 3.2 cm/s (MMI IV–V) and a factor of 3.1, respectively. Overall, the highest basin amplification (largest surface waves) generated across Greater Vancouver is associated with earthquakes located ≥ 80 km south-southwest of the city. The area of basin-amplified motion (≥ 2.5) is primarily associated with the lowest velocity sediments (V_s ≤ 1.0 km/s) at 250 and 500 m depth surfaces of the model.

Limitations of this work include: (1) uncertainty in accuracy of physical-structure and source-rupture models; (2) omission of low-velocity (V_s < 625 m/s) materials in the 3D structure models, such as water and up to 300 m of Holocene Fraser River delta sediments, as well as surface topography; and (3) inability to resolve frequencies > 0.5 Hz. The updated 3D physical-structure model can be further improved by: (1) incorporation of the 600 m gridded V_p model of Dash et al. (2007); only the 800 m surface was used here), (2) validation by comparison with future empirical earthquake recordings, and (3) increasing the maximum depth to ~80 km for simulation of JdF plate earthquakes (constrained to maximum depth of 55 km here). Conclusions are limited to the simulations conducted here and are specific to the chosen epicenter locations and earthquake rupture style. However, conclusions as to the overall most hazardous deep JdF plate scenario earthquake (within 100 km of Greater Vancouver) are relatively robust because the most likely locations and rupture style of such an event have been considered here. Overall, this study shows that the presence of 3D Georgia basin structure increases the level and duration of predicted long-period ground shaking, effects that are linked to potential earthquake damage.

Data and Resources

Subvolumes of the Pacific Northwest Community Velocity Model (v. 1.3) of Stephenson (2007) are used for the 3D modeling. Velocity data supplication provided by Jim Hunter (Natural Resources Canada [NRCAN], Ottawa), Stephen Glover (British Columbia Ministry of Energy, Mines and Petroleum Resources), David Mosher (NRCAN, Atlantic), and Ranjan Dash (Chevron). Earthquake recordings of the 2001 Nisqually earthquake used in this work were retrieved from online catalogs of the Pacific Northwest Seismic Network at ftp://ftp.geophys.washington.edu/pub/seisnet/OLYMPIA/ (last accessed November 2013) and ftp://ftpext.usgs.gov/pub/crc/golden/hazards/Carver/Seattle/SEAascii200001to200409/20010228185444/ (last accessed November 2013) and from the Canadian National Seismic Network at http://earthquakescanada.nrcan.gc.ca/stndon/AutoDRM/autodrm_req-eng.php (last accessed March 2009). The Anelastic Wave Propagation–Olsen Day Cui (AWP–ODC) finite-difference simulation code was used for the 3D simulations. Software used to update the 3D velocity structure model includes ArcGIS (ESRI) and ParaView (open source). Maps and time snapshots of FD simulations were generated using MATLAB (MathWorks) software; coordinates of the North American coastline were obtained at http://www.ngdc.noaa.gov/mgg/coast/ (last accessed August 2010). Waveforms filtered and plotted using Seismic Analysis Code (Incorporated Research Institutions for Seismology) software.

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